

The Digital Economist

Intermediate Macroeconomics

Worksheet #6: **The Algebra of Demand-Side Equilibrium** Name: _____

Product Markets:

$$AE_t = C_t + I_t + G_t + NX_t$$

$$Y_t = AE_t$$

Aggregate Expenditure
Equilibrium condition {Income = Expenditure}

$$C_t = b(Y_t - tY_t)$$

Consumption Expenditure
{ $0 < b < 1$, $b = \text{MPC}$, $t = \text{income tax rate}$ }

$$I_t = I_0 - h(r)$$

$I_0 = f(\text{RGDP, Price of Capital, Productivity of Capital})$
{ $h = \text{interest sensitivity of Investment Exp.}$ }

$G_t = G_0$
variable

Government Expenditure – A policy

$$NX_t = EX_0 - IM_0$$

$$EX_0 = f(\text{e.r.})$$

$$IM_0 = \begin{matrix} (-) \\ (+) \end{matrix} f(\text{e.r.})$$

Net Export Expenditure
{e.r. = exchange rate -- $\text{€}/\text{\$}$, $\text{P}/\text{\$}$, ...}

$$AE_t = b(Y_t - tY_t) + I_0 - h(r) + G_0 + NX_t$$

$$= [A_0 - h(r)] + b(Y_t - tY_t) \quad \{A_0 = I_0 + G_0 + NX_t\}$$

note: $[A_0 - h(r)]$ defined as *Autonomous Exp.*

in equilibrium,

$$Y_t = [A_0 - h(r)] + b(Y_t - tY_t)$$

or

$$Y_t - b(Y_t - tY_t) = [A_0 - h(r)]$$

or

$$Y_t[1 - b(1 - t)] = [A_0 - h(r)]$$

or

$$Y_t^* = \alpha[A_0 - h(r)] \quad \text{where } \alpha' = \frac{1}{[1 - b(1 - t)]} \dots \text{the spending multiplier}$$

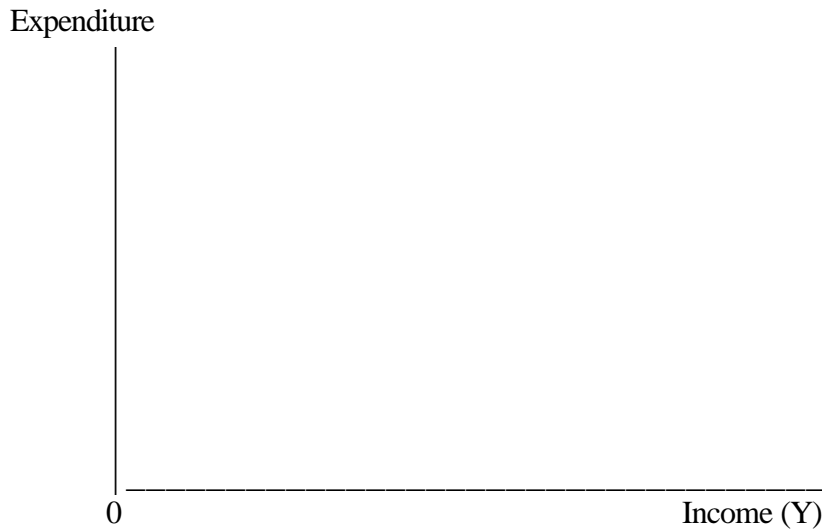
1. Given the following equations:

$C_t = 0.75(Y_t - T)$	<i>Consumption Expenditure</i>
$I_t = 200 - 500(r)$	<i>Investment Expenditure</i>
$G_t = 250$	<i>Government Expenditure</i>
$NX_t = 100$	<i>Net-Export Expenditure</i>
$T = 0.20Y_t$	
$Y_t = C_t + I_t + G_t + NX_t$	<i>Equilibrium Condition</i>

a. Determine the following:

- i. the Marginal Propensity to Consume: _____
- ii. the Interest Sensitivity of Investment: _____
- iv. the (Income) tax rate: _____
- v. the level of Autonomous Expenditure for $r = 0.10$: _____
- vi. the Spending multiplier: $\{1/[1-b(1-t)]\}$: _____

b. find the level of equilibrium income for a market interest rate of 10% ($r = 0.10$) and graph this relationship in the diagram below:



c. Given this equilibrium level of income, calculate the level of tax revenue collected: _____ Is the government running a surplus or deficit?: _____

d. Calculate the level of savings: _____ and investment expenditure: _____ at the equilibrium level of income. Is there a funds (savings-investment) surplus or deficit? _____ How are these surplus or deficit funds being used? _____

2. Suppose that Income is fixed at **\$1000**. Using the equations of page 2, calculate the corresponding value of the real interest rate, investment expenditure, savings, and the budget deficit.

How will a \$50 ($\Delta G = 50$) increase in government spending impact the real interest rate?

How does this shock affect: savings, investment expenditure, and the budget surplus/deficit.

3. The equilibrium condition can be rewritten as follows:

$$Y_t^* = \alpha[A_0 - h(r)]$$

solving for 'r':

$$r = A_0/h - (1/\alpha h)Y_t$$

Using the equations of page 2 graph the equilibrium condition in the diagram below:

